

Title:	Resonance in Transverse Waves  1 July 2004 4 April 2008  Charlene Rydgren, Jeff Harbold, George Wolfe, Joan Taber, Marty Alderman  Regents Physics				
Original: Revision:					
Authors:					
Appropriate Level:					
Abstract:	This experiment is designed to develop the student's understanding of resonance. Students explore the conditions needed to establish standing waves on a string and discover the relationship between nodes and antinodes for different resonant modes. Students also determine the relationship between frequency and wavelength for a fixed length of string.				
Time Required:	One 40-minute period for lab activities. If experimental design and post-lab analysis are done in class, two more class periods are needed.				
NY Standards Met:	<ul> <li>4.3c The model of a wave incorporates the characteristics of amplitude, wavelength, frequency, period, wave speed, and phase.</li> <li>4.3f Resonance occurs when energy is transferred to a system at its natural frequency.</li> <li>4.3m When waves of a similar nature meet, the resulting interference may be explained by the principle of superposition. Standing waves are a special case of interference.</li> </ul>				
Special Notes:	Resonance is a kit available through the CIPT Equipment Lending Library, Xraise.classe.cornell.edu  Created by the CNS Institute for Physics Teachers via the Nanoscale Science and Engineering Initiative under NSF Award # EEC-0117770, 0646547 and the NYS Office of Science, Technology & Academic Research under NYSTAR Contract # C020071				

#### **Behavioral Objectives:**

Upon completion of this lab activity, a student should be able to:

- Explain that standing waves only occur at special frequencies called resonant frequencies.
- Be able to use the wave equation  $v = f\lambda$  to solve for the velocity of a standing wave in a fixed-length string.
- Explain the relationship between the nodes and antinodes of a standing wave and its wavelength.

#### **Class Time Required:**

One 40-minute class period. If analysis and experimental design are done in class, two more class periods are needed.

## **Teacher Preparation Time:**

15 minutes

## **Assumed Prior Knowledge of Students:**

Wave equation  $v = f\lambda$ 

Constructive and destructive interference

#### Tips for the Teacher:

- It is highly recommended to use the power supply with the LabPro, due to its high consumption of power. If battery power must be used, use the following procedure to avoid wasting batteries: when done using the LabPro disconnect the photogate, quit the DataGate software, and turn off the calculator. The best way to ensure that the LabPro is off is to remove one of the batteries. Even when all devices appear to be turned off, the batteries may still drain.
- If the motor is turned on but not rotating, move the speed control knob to the maximum speed. The motor will usually start spinning. Then you can adjust the motor to the desired speed.
- Remind students to turn off the motors when not in use.
- If your students have not used a photogate before, you will want to explain how it works. The photogate has an infrared light source and an infrared detector separated by an open space. As the string passes through that space, the gate's light path is interrupted. The small red LED on the photogate will light to indicate that the beam is being interrupted by the string. The LabPro or LabQuest determines the time between passes, averages these for 10 oscillations, and returns the period of vibration to the nearest .001 second.
- When the students are using the photogates, emphasize that the infrared beam of the photogate should be centered on the motion of the string. If the beam is positioned on the edge of the string's motion, the photogate may report twice the actual period.
- You may also want to remind your students about standard deviation. The photogate returns the standard deviation for the 10 period measurements. If the standard deviation is more than ~1 x 10<sup>-4</sup> in this experiment, then the trial should not be recorded. Standard deviation is a measure of the spread of data, and a large spread indicates a likely error in the measurement. Errors can be caused by a swinging motor or a photogate that is not centered on the motion of the string. Emphasize that if the standard deviation is too high, students should try to steady the motor unit, and/or adjust the position of the photogate; then run the trial again.
- It may be useful to do a review of the wave equation with students. Below is a derivation of the wave equation.

- $\circ$  For motion with a constant velocity v, one uses x = vt where x is the distance and t is the time traveled.
- o The speed of a wave is constant within a given medium, and one cycle of a wave will move its wavelength ( $\lambda$  = the distance for one cycle) in its period (T = the time for one cycle), making the simple motion equation applied to a wave become:  $\lambda = vT$
- $\circ$  Recall that period and frequency are reciprocals of each other. Replace **T** in the last equation with **1/f**, and rearrange the equation. It becomes the familiar **v** = **f**λ

# **Equipment List**

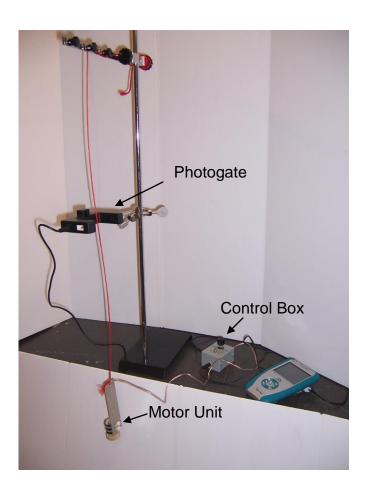


Photo ID	No.	Item
1	1	Vernier Lab Pro Interface ***
2	1	TI-83 Plus calculator
3	1	Pendulum clamp
4	1	Connector cable
5	1	Vernier Photogate
6	1	Vernier LabQuest ***
7	1	Resonator unit
Not in picture		Ring stand with cross bar

<sup>\*\*\*</sup> Note – You need either the Vernier Lab Pro Interface and TI-83 Plus Calculator or the Vernier LabQuest, but not both to complete this lab.

#### RESONANCE IN TRANSVERSE WAVES

Waves come in two main varieties: transverse and longitudinal. When you drop a pebble in a lake, the ripples spread outward along the surface, while a blade of grass on the surface bobs up and down. The water molecules oscillate up and down, moving vertically between extreme positions, and carrying the blade of grass up and down with them. Meanwhile, the wave propagates (moves) horizontally out along the surface. Since the motion of the water molecules is perpendicular to the propagation direction of the wave (and the direction of energy flow), such waves are called *transverse* waves. (The prefix 'trans' means 'across'). In contrast, the displacement is parallel to wave propagation axis for longitudinal waves. In this lab you will explore transverse waves. As you will see, a wave on a string is a transverse wave, since the string oscillates perpendicular to its axis.

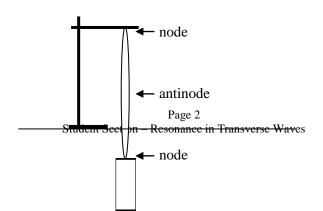


## **Standing Waves**

- Loop the string of the motor unit over the arm of the pendulum clamp to obtain the longest string length possible.
- Set the control box on a chair or bench nearby so that the wire hangs loosely draped between the motor unit and the control box. It is ok for the control box wires to touch the floor.
- Turn on the motor and set it to a medium to slow speed. Pull the free end of the string to slowly raise the motor unit. Stop pulling and secure the string when a half-wave appears in the string.
- 1. Look around. Are all the string lengths that form a half-wave the same length? \_\_\_\_\_\_
- 2. Other than length, how is your system different from other systems in the room?
- 3. Change the frequency of vibration of the motor unit by adjusting the speed control. What happens to your half-wave?
- 4. Predict how you can re-form your half-wave without changing the vibration rate of the motor unit.
- 5. Test your prediction. What did you do to re-form your half-wave?
- 6. The wave you have been observing is called a "standing wave." Why do you think this term was chosen?
- 7. When a system is driven at a special frequency, called its "natural frequency," it has a large amplitude response. This is known as "resonance." Are standing waves an example of resonance? Explain.

## **Nodes and Antinodes**

Although a standing wave appears to stand still, it is actually made from traveling waves moving in opposite directions along the string. When there is a standing wave, complete destructive interference occurs only at certain locations called <u>nodes</u>, where the medium barely moves at all. Maximum constructive interference occurs at locations called <u>antinodes</u>, where the medium oscillates with maximum amplitude. The simplest standing waves in the string have two nodes, one at each end, as in the diagram below.



- Clamp the string to the stand so that it hangs almost to the floor, and set the speed of the motor to roughly 2/3 of full speed.
- Pinch the string between your thumb and forefinger to create a 'finger-clamp' on the string. Slide your finger-clamp down the string until you create a standing wave.
- By changing the effective string length in this fashion, form a standing wave with only three nodes. Note how this resembles a full cycle of a wave, or one wavelength.

If three nodes produce a complete wavelength as you see here, what is the distance between two

Δ.	nodes in terms of wavelength? wavelength
2.	How many antinodes are there with three nodes? Two nodes?
3.	How many wavelengths fit on a string with <i>four</i> nodes? wavelength
4.	Have your partner grab the node in the middle. Describe what happens to the portion of the standing wave below his or her fingers.
5.	Is it possible to get a standing wave with 1/4 or 3/4 of a wave-length on the string? Explain.
•	Turn off the motor.

## Resonant modes of a fixed-length string

By now, you will have noticed that resonance (standing waves) only occurs for special conditions. You will determine what these special conditions are for a fixed-length string. In the first part of the lab, you changed the length of the string. However, it often happens that the wave medium (in this case, the string) is a fixed length.

Question: What are the conditions that create standing waves (resonances) on a fixed-length string?

## **Experimental Design:**

- 1. List all the variables (physical quantities that can change) in the motor/string system.
- 2. Which of the variables you listed in 1. will you keep constant in this experiment?
- 3. Which of the variables you listed in 1. will you change, or allow to change?

- 4. Given a photogate<sup>1</sup>, a meterstick, and anything else in the room, how will you measure each of the variables?
- 5. Design a procedure aimed at answering the Question above, using what you wrote in 1.-4.

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As you follow the steps below, note the similarities and differences between this procedure and the one you proposed.

vibrating

string

motor

center photogate

beam on motion

of string

- Turn on the motor and set it to as low a speed as practical.
- Pull the free end of the string to slowly raise the motor unit. Stop pulling and secure the string when the largest amplitude, half cycle standing wave (2 nodes) appears in the string.
- Measure the string length between the nodes and record it in the data table on page .
- To measure the period of the wave, place the photogate as close to an antinode as possible (where the sting moves most). Make sure that the motor unit is hanging without swinging. Then carefully center the beam of the photogate on the motion of the string.
- Using the appropriate photogate instructions in the box below, measure the period of the wave and the sample standard deviation. If the standard deviation is less than 1 x 10<sup>-4</sup>, record the information in the data table. If not, steady the motor unit, adjust the photogate position, and repeat the trial.

position

antinode

photogate at

- Record the period and the standard deviation in the data table. Keeping the same string length, adjust the motor speed until 3 nodes appear, reposition the photogate to an antinode, measure the period and measure the distance between nodes. Record your data in the table.
- Establish resonance with four nodes and five nodes and take the data as you did for 3 nodes.
- Turn off the motor.
- Turn off the LabQuest or LabPro.

<sup>&</sup>lt;sup>1</sup> A photogate is an electronic timer containing a light beam. Every time an object blocks the light beam, the timer starts or stops.

# **DIRECTIONS FOR USING THE PHOTOGATE With LabQuest**

- Connect the power supply.
- Plug the photogate sensor into the DIG1 input of the LabQuest unit.
- Turn on the LabQuest.
- On the "File Sensors" screen, select timing.
- Set Photogate mode to Pendulum.
- Click OK.
- Press the Play/Stop button once to start the system.
- Press the Play/Stop button again to stop the system after roughly 10 seconds.
- Se DIRECTIONS FOR USING THE PHOTOGATE With LabPro
- Select Statistics from the danual amenie Vernier LabPro are connected and
- Sakedinhth Period dook ling in appearab Pro and turn on the calculator.
- Connect the Phringhtelto the LabPro. Insert the white end of the cable into the "Dig/Sonic 1" slot on the LabPro and the other end into the opening on the photogate.
- Turn on the calculator and press "PRGM."
- Select "DATAGATE."
- Press "ENTER."
- Press "1" to go to SETUP.
- Press "3" for PENDULUM. (Do not select the PHOTOGATE option, as PENDULUM works best here.)
- Press "2" for START.
- Press "STO" when finished.

#### Data table

Overall length of string from suspension point to motor unit =

Number	Distance	Wavelength	Period of	Standard	Frequency	Wave speed in
of nodes	between	λ in (m)	vibration	deviation of	f in (Hz)	the medium
	adjacent		T in (s)	period		(the string)
	nodes (m)			σ in (s)		v in (m/s)
2						
3						

4			
5			

# Post-lab Analysis

- 1. You measured the period of the oscillation and the distance between the nodes. Calculate the frequency and the wavelength for each resonance from this information, and record the results in the data table.
- 2. Look at the frequency column in your data table. How are the frequencies of the different resonant modes related to the frequency of the first (fundamental) mode?
- 3. If you were to make a standing wave with 6 nodes, predict the frequency that would produce this resonance, assuming the same length of string. Show your work.
- 4. Look at the wavelength column in your data table. How are the wavelengths of the different resonant modes related to the wavelength of the fundamental mode?
- 5. If you were to make a standing wave with 6 nodes, predict the wavelength of this resonance, assuming the same length of string. Show your work.
- 6. Your motor can only explore a limited range of frequencies. If you had a motor that could vibrate at any frequency, would you expect to find any additional resonant modes at lower frequencies? At higher frequencies? Explain your answer.
- 7. Use  $v = f\lambda$  to fill in the remaining column in the data table. Use those values to make your best estimate of v, the speed of the waves on the string.
- 8. Does the velocity of the waves change significantly or remain essentially constant? Do you expect the velocity to change? Explain your reasoning.

- 9. From your values for v, predict the length of string that would resonate at 75 Hz with two nodes. Explain your reasoning.
- 10. You learned in this lab that the wave speed in the string stayed constant. With the help of the following equation, list two ways you could increase the wave speed of a string.

$$\upsilon=f\lambda=\sqrt{\frac{\tau}{\mu}}$$
 where  $\tau$  = tension of the string and  $\mu$ = mass/unit length of the string